K₃Ti₈O₁₇, a New Alkali Titanate Bronze

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A new alkali titanate oxide bronze $K_3 Ti_8 O_{17}$ has been prepared by fused oxide electrolysis at 1010°C. It is monoclinic, space group C2/m, with unit cell dimensions a = 15.68, b = 3.809, c = 12.06 Å, $\beta = 95.0^{\circ}$. Its structure is defined by a framework of titanium-oxygen octahedra and at any one level the octahedra edge-share in blocks of four with their diagonals directed along the 3.8 Å c axis. Each block edge-shares to similar blocks above and below it to form zigzag ribbons of closely packed octahedra. The ribbons are corner joined to similar units to form staggered sheets which join still further to form prismatic tunnels which contain potassium atoms side by side in groups of three. The structure is closely related to two known sodium titanates $Na_2 Ti_6 O_{13}$ and $Na_2 Ti_7 O_{15}$.

Introduction

Oxide "bronzes" form a special group in the families of oxide compounds. They have a threedimensional framework of metal-oxygen polyhedra in which all metal sites are occupied, and which encloses crystallographically defined sets of positions that are partly or wholly occupied by other metal ions. These ions are commonly those of the alkali or alkaline earth metals but may include Al³⁺, In³⁺ or the trivalent rare earths. In all cases variations in the occupancy of the "enclosed" sites is charge compensated in the host framework. For normal insulating oxides this compensation involves alterations in compositional ratios, e.g., in titanates such as $Cs_xMg^{2+}Ti_{2-x/2}^{4+}O_4$ or $Cs_xFe^{3+}Ti_{2-x}^{4+}O_4$, the Mg^{2+}/Ti^{4+} or Fe^{3+}/Ti^{4+} ratios alter with x. In the case of bronzes however, charge compensation is achieved by a reduction in valency of a fraction of the host metal ion, e.g., $Na_x TiO_2(l)$ may be regarded formally as $Na_x(Ti_x^{3+}Ti_{1-x}^{4+})O_2$. Bronzes can be prepared in a number of ways notably by electrolysis (2) and (3), but except for those of vanadium, do not as a rule appear during a normal phase study. A recent review by Banks and Wold (2) emphasizes the need for reducing conditions in the preparation of bronzes. Two titanium bronze compounds have been identified among the products obtained by reducing various alkali titanates in hydrogen (1); one was $Na_{x}TiO_{2}$ which has a unique structure and the other $K_x TiO_2$, which with the Rb and Cs analogues is isomorphous with the mineral hollandite

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(4). Subsequently the sodium titanium bronze was synthesized by solid state reaction in the ternary system $Na_2Ti_3O_7$ -Ti O_2 -Ti (5).

As reported elsewhere in this journal we have studied the electrolysis of fused oxide systems based upon $K_2Ti_2O_5$ (6). We were able to synthesize K_xTiO_2 (hollandite) from pure molten $K_2Ti_2O_5$ and $K_2Ti_2O_5$ -TiO₂ systems, but the same melts with 1.5-2.0% Nb₂O₅ added gave a "bronze" with a different structure. The present work establishes that this new bronze has a composition $K_3Ti_8O_{17}$ and a structure very close to that predicted by Wadsley and Mumme (7) for the hypothetical titanate "Na₂Ti₈O₁₇." The theory is also discussed that the large polyanions which form the basic building blocks of this and similar bronzes probably exist in oxide melts prior to their aggregation in crystalline form.

Experimental

The apparatus used for the preparation of the bronze is described in detail elsewhere in this journal (6). The melt composition used in the initial preparation was 30.3 mole% K₂O (as K₂CO₃) 68.2 mole% TiO₂ and 1.5 mole% Nb₂O₅. The melt was electrolysed under argon at 1010°C for 16 hours at a current of 60 mA/cm². The resulting cathode deposit appeared grey in colour, but when viewed under the microscope it contained individual black needle-like crystals up to 0.5 mm in length embedded in the colourless melt. The needles were separated

from the melt by dissolution of the latter in warm 1:1 HCl. In a further preparation carried out at a higher mole fraction of Nb₂O₅ (1.90 mole %) at a temperature of 1030°C and at 100 mA/cm², the same product was obtained. However, upon lowering the temperature to 990°C at both these compositions, the main phase isolated from the cathode was potassium hollandite (K_xTiO₂) and only very small amounts of the bronze were present.

Electrolysis of a melt containing K_2O and TiO_2 in the mole ratio 1:2 at temperatures of 1020, 1030, and 990°C and at various current densities gave only crystals of K_xTiO_2 .

Results

The black needle-like crystals of the bronze were found to have monoclinic symmetry with the crystallographic constants given in Table I. The cell dimensions were determined from single crystal data together with a refinement of the b axis with the Guinier powder data given in Table II. Initial chemical analysis was not undertaken because it could be seen that there was a strong resemblance between this phase and the hexa- and heptatitanates (7) and (8). The potassium content was found subsequently by the procedure detailed in the structural analysis and the final composition limits were determined by the space group point positions. No reliable measurement of the density could be made as it proved difficult to isolate sufficiently large quantities.

Intensity data h0l to h3l were recorded on multiple films with CuK α radiation using an integrating Weissenberg goniometer. Intensity measurements were made visually by comparison with a

TABLE I

CRYSTALLOGRAPHIC DATA FOR K3Ti8O17

Symmetry:	monoclinic			
Unit cell dimensions:	$a = 15.68 \pm 0.01$ Å			
	$b = 3.809 \pm 0.003$ Å			
	$c = 12.06 \pm 0.01$ Å			
	$\beta = 95.0^{\circ}$			
Systematically absent reflection	s: hk' with $k + k \neq 2n$			
Possible space groups:	C2/m (No. 12), Cm (No. 8),			
	C2 (No. 5)			
	$Dc = 3.57 \text{ g cm}^{-3}$			
	Z = 2			
	$\mu_{\rm c} = 480.5 \ {\rm cm^{-1}}$			

TABLE II

GUINIER POWDER PATTERN OF K3Ti8O17

$CuK\alpha_1$ Radiation					
hkl	$\sin^2 \theta_{obs}$	$\sin^2 \theta_{calc}$	I		
110	0.04330	0.04333	VS		
310	0.06281	0.06282	MS		
31 Ī	0.06532	0.06525	Μ		
201	0.07113	0.07111	MS		
113	0.08201	0.08208	VW		
403	0.08252	0.08248	S		
60Ī	0.08830	0.08835	VW		
114	0.10670	0.10677	VVW [.]		
403	0.13076	0.13072	W		
020	0.16358	0.16355	Μ		

standard scale. The physical dimensions of the crystal were $0.52 \times 0.06 \times 0.03$ mm, and no absorption corrections were considered necessary. Scattering curves for neutral Ti and K were taken from International Tables of X-ray crystallography (9). Suzuki's (10) value for O²⁻ were used for oxygen. All calculations were made on an Elliott 803 Computer with the aid of programs from Daly, Stephens and Wheatley (11).

Structure Determination

The Patterson projection P(u, w) consisted of parallel rows of peaks at approximately 15° from the positive direction of the a axis, and bore a strong resemblance to the Patterson function of Na₂Ti₇O₁₅ (7). It was assumed that the *b*-axis length of 3.81 Å corresponded to the octahedral body diagonal and the ideal structure for the new bronze was drawn up to scale along the [010] direction and used as the initial basis for the structure determination. Vector coincidences were found to occur at 3.0-3.2 Å, corresponding to edge shared octahedra at the same level in periods of four and other coincidences corresponded to edge shared octahedra at different levels. This procedure of determining vectors representing complete octahedra and not just atoms, developed by Wadsley and co-workers (12) and (13), lead to a nearly definite solution of the structure, with the two potassium atoms K(1) and K(2) placed initially in the 2(d) and 4(i) positions of the space group C2/m.

The ideal parameters for titanium and oxygen together with those for the two potassium atoms were taken from the model for structure factor TITANATE BRONZE

TABLE III

h	k	l	£	Ę	(h	k	l	Ê	Ę	h	k	ł	Ę	Ę	
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* Affected by extinction.



FIG. 1. Structure of K₃Ti₈O₁₇. Smallest circles Ti, largest O, intermediate stippled K.

calculations using the h0l level data. Electron density maps along the [010] direction were used to refine these parameters and final structure factor calculations using all the three-dimensional data gave after refinement a reliability value of 18.0. Closer observation of the electron density projections indicated that the peak due to the potassium atom K(1) was elongated across the centre of the cell. Shifting this atom to the fourfold 4(i) position with a corresponding decrease in the scattering power to $\frac{1}{2}$ K, rapidly reduced the R value to 11.8 and also decreased the isotropic temperature factor for K(1) from 5.5 to 1.8 $Å^2$. Therefore, the compound possesses the limiting formulae K₃Ti₈O₁₇ with a formal charge distribution given by $K_{3}Ti^{3+}Ti^{4+}O_{17}$. It is possible that statistically less than three potassium atoms occupy each unit cell with a consequent decrease in the Ti^{3+}/Ti^{4+} ratio. As correctly predicted by Wadsley and Mumme (7), the basic framework of the structure is built up from four octahedra sharing edges at one level, which combine with similar units above and below into zigzag ribbons of octahedra.

The ribbons are joined to similar units by corner sharing to form staggered sheets which are further joined to form prismatic tunnels in which the potassium atoms are situated. The potassium atom K(1) is randomly distributed in its 4(i) position and the 4(i) sites containing the K(2) atoms are fully occupied.

A comparison of observed and calculated structure factors are given in Table III. The structure is illustrated in Fig. 1 as a ball and spoke model showing half potassium for K(1). Final atomic parameters are given in Table IV, the standard

TABLE IV

Fractional Atomic Parameters for $K_3Ti_8O_{17}$ Space Group C2/m E.S.D./s in Parentheses

	Point position	x	у	z	β(Ų)
1 <u></u>	4 (i)	0.4871 (22)	0	0.46102 (6)	1.7 (6)
K (2)	4 (i)	0.4429 (9)	0	0.1715 (2)	1.0 (2)
Ti (1)	4 (i)	0.1134 (7)	0	0.0736 (8)	0.5 (2)
Ti (2)	4 (i)	0.1484 (7)	0	0.3249 (9)	0.5 (2)
Ti (3)	4 (i)	0.1984 (8)	0	0.5769 (9)	1.0 (2)
Ti (4)	4 (i)	0.2457 (7)	0	0.8311 (9)	0.8 (2)
O (1)	2 (a)	0	0	0	1.8 (1.3)
O (2)	4 (i)	0.064 (2)	0	0.230 (3)	0.2 (6)
O (3)	4 (i)	0.103 (3)	0	0.461 (4)	1.0 (8)
O (4)	4 (i)	0.144 (4)	0	0.713 (5)	2.7 (1.2)
O (5)	4 (i)	0.172 (3)	0	0.931 (4)	1.3 (9)
O (6)	4 (i)	0.233 (3)	0	0.191 (4)	2.3 (1.1)
O (7)	4 (i)	0.279 (2)	0	0.433 (3)	0.0 (6)
O (8)	4 (i)	0.317 (3)	0	0.678 (4)	2.0 (1.0)
O (9)	4 (i)	0.361 (2)	0	0.913 (3)	0.0 (7)

Metal	Bonds to oxygen atoms	Distances Å	Average	Average O–O distances Å
Ti (1)	9' (2); 5', 6, 2, 1	1.95 (2), 2.04 2.25 2.10 1.92	2.03	2.86
Ti (2)	8' (2); 7, 6, 3, 2	1.98 (2), 2.33 2.18 1.85 1.67	2.00	2.78
Ti (3)	7' (2); 8, 7, 4, 3	1.94 (2), 2.14 2.24 1.92 1.95	2.02	2.84
Ti (4)	6' (2); 9, 8, 5, 4	1.96 (2), 1.99 2.25 1.74 2.05	1.99	2.79

TABLE V Interatomic Distances for Ti Octahedra in K_3 Ti $_8$ O $_{17}$ E.S.D. for Ti–O Distances ±0.10 Å and O–O Distances ±0.15 Å

Number followed by (2) and semicolon refers to atoms lying above and below the metal.

temperature factors being averaged out for atoms of the same kind. The Ti–O separations, listed in Table V, show a wider spread of distances than observed in the sodium titanates, $Na_2Ti_6O_{13}$ (8) and $Na_2Ti_7O_{15}$ (7). The short Ti–O bonds of 1.57– 2.00 Å found in $K_2Ti_2O_5$ (14) were attributed to the possible repulsion between nearest-neighbour metal atoms. In $K_3Ti_8O_{17}$ the oxygen atoms of the two short Ti–O bonds, 1.67 and 1.78 Å, also form part of the K(1) atom coordination sphere and repulsion between the potassium atoms may well have the effect of decreasing these two Ti–O bond lengths.

The two kinds of potassium atoms differ in their coordination with oxygen. K(1) has four short bonds, two at each of 2.60 and 2.64 Å to form a nearly square planar $K-O_4$ configuration. The next nearest oxygens are at distances of 3.39 Å (2) and 3.60 Å(2) and are therefore nonbonding. A similar coordination has been observed for one of the sodium atoms in $Na_2Ti_7O_{15}$ (7). K(2) on the other hand is essentially eight coordinate. The six shorter bonds, two at each of 2.78, 2.83, and 2.74 Å, have an average length of 2.78 Å, equal to the average eightcoordinate K-O distances found in scheelite-type structures KBO_4 , where B is Ru (15), Re (16) or I (17). The two additional bonds K(2)-O(1) are longer because the oxygen atoms are constrained in special positions. This has also been observed in $Na_{2}Ti_{6}O_{13}(8)$.

Discussion

The original aim of the preparative experiment was the formation of a mixed $Nb^{4+}-Ti^{4+}/Ti^{3+}$ alkali-metal oxide. The oxide phase that formed in all the experiments appeared to contain relatively little niobium, as several crystals prepared from melts with different niobium contents gave exactly the same diffraction data. No immediate reason can be put forward as to why the presence of Nb₂O₅

is necessary for the formation of the bronze. It has been shown however that Nb⁵⁺ substitutes isomorphously for Ti⁴⁺ in the compounds KTiNbOs and KTi₃NbO₉ (18) and therefore some Nb⁵⁺ may be randomly substituted for Ti⁴⁺ in K₃Ti₈O₁₇, with a corresponding increase in the Ti³⁺/Ti⁴⁺ ratio, to give a phase of composition $K_3 Ti_{1+x/2}^{3+} Ti_{7-x}^{4+} Nb_{x/2}^{5+} O_{17}$ with $x \ll 1$. Similar stabilization phenomena has been observed for several other alkali metal titanate systems. For example, sodium heptatitanate (7) was formed by solid state reaction in the presence of a high percentage of Al_2O_3 , and in the electrolysis of certain Na_2TiO_3 -TiO₂ melts (6), a bronze phase was readily formed with Al₂O₃ in the melt, but not when it was absent. When a different Group V metal, oxide namely V_2O_5 , was added to a K₂Ti₂O₅-TiO₂ melt electrolysis resulted in the formation of a new phase (19) of composition close to $K_{0.8}V_{0.8}Ti_{1.2}O_4$, with a layer structure related to that of rubidium manganese titanate (20).

As predicted by Wadsley and Mumme (7) the stoichiometric octatitanate $Na_2Ti_8O_{17}$ had the same arrangement of 4×1 blocks of Ti-O₆ octahedra as presently found in K₃Ti₈O₁₇, except that in their model the Na atoms occupied two-thirds of the 4(i) positions and two of the twofold positions corresponding 2(d) in the space group C2/m. The potassium atom K(1) in $K_3 Ti_8 O_{17}$ was found to be displaced from the idealized 2(d) position and randomly distributed in the tunnels in the 4(i) positions, with the other potassium K(2) in the same environment as originally suggested. The relatively large isotropic temperature factors for the potassium atoms can be attributed to their unhindered motion in the tunnel directions and the value of 1.2(6) Å² for K(1) is not abnormal. B for Na in Na₂Ti₆O₁₃ (8) was found to be 2.3 $Å^2$.

The relationships between the hexatitanate, heptatitanate and the present octatitanate phase



FIG. 2. Idealized structures of $K_3 Ti_8 O_{17}$ in projection on to (010). The squares are Ti-O octahedra; the heavy and light outlines represent the two levels in the unit cell.

have been discussed by Wadsley and Mumme (7). Figure 2 shows the idealized arrangement of Ti–O octahedra for $K_3Ti_8O_{57}$ as postulated by these workers. All three of these phases are built up in the solid state from 3×1 or 4×1 blocks of edge shared octahedra which join by corner sharing to give a step-like configuration as shown. In the parent compound $Rb_xMnTi_{2-x}O_4$ (20) discrete blocks of Ti–O₆ octahedra do not form and the structure consists of infinitely extended layers of edge shared octahedra.

The outstanding common structural feature of all these titanates are the polyhedral groups of $Ti-O_6$ octahedra with their diagonals directed along the baxis of their unit cells and repeating infinitely in this direction. Some of these polyhedral ribbons or sheets may be regarded as being built up from separate polyanionic groups of a general formulae $(Ti_nO_{2n+1})^{2-}$, n > 1, as in the dititanate, $(Ti_2O_5)^{2-}$ n = 2, trititanate $(Ti_3O_7)^{2-}$ n = 3 and hexatitanate $(Ti_6O_{13})^{2-}n = 6$ (n is not necessarily the same as the block width which, for $Na_2Ti_6O_{13}$ is 3). Such polyanions have been found as structural features of other alkali metal bronzes. For example the two potassium molybdenum bronzes $K_{0.26}MoO_3$ (21) and $K_{0.28}MoO_3$ (22), prepared from electrolysis of K_2O-MoO_3 melts (3) were shown to contain large ions of the type $Mo_6O_{22}^{8-}$ and $Mo_{10}O_{36}^{12-}$ as their basic frameworks (21) and (23). These ions are made up of Mo-O octahedra united by edge and corner sharing to form infinite sheets of polynuclear groups similar to those found in $K_3 Ti_8 O_{17}$ and related alkali titanates. These polyanions have a strong resemblance to the isopolymolybdate anions, $Mo_8 O_{26}^{4-}$ and $Mo_7 O_{24}^{6-}$, found in molybdates prepared from solutions (24).

The formation of large complex anionic species in various solutions and melts has been the subject of numerous studies. The investigations by Flood and Knapp (25) of silicate melts containing Group IVA metal oxides are relevant to the present molten titanate systems. These workers were able to calculate the stability in melts of certain silicate ions such as $(SiO_{2.5})_{6}^{6-}$ by determining the activity of SiO₂ and applying the concepts of acid-base equilibria. Recently, these concepts have been applied to determine the heats of solution of MoO₃ in molten Na₂MoO₄, in terms of the formation of anions such as $(Mo_nO_{3n+1})^{2-}(26)$.

The existence in the solid state of large polymeric groups as the basic building blocks of bronzes and titanates suggests that such groups may also be present in the oxide melts from which the compounds have been prepared. The existence, domain of stability and character of these anions will depend upon the activity of the host metal oxide as well as the acid-base equilibria and O^{2-} ion activity in the melt. For example the formation of the anion $(Ti_2O_5)^{2-}$ may proceed through the formation of the intermediate $[Ti_2O_{10}]^{12-}$ according to the following reaction using Flood and Förland's (27) original proposal of acid base equilibrium in molten oxides.

$$\begin{array}{rcl} 60^{2-} + 2\text{TiO}_2 &\rightleftharpoons [\text{Ti}_2\text{O}_{10}]^{12-} &\rightleftharpoons [\text{Ti}_2\text{O}_5]^{2-} + 50^{2-}\\ \text{[acid]} & \text{[base]} \end{array}$$

the O^{2-} ion arising from the ionization of K_2O

$$K_2O \rightleftharpoons 2K^+ + O^{2-}$$

In the present case the formation of the potassium octatitanate bronze by the electrochemical reduction of molten $K_2Ti_2O_5$ -TiO₂ may have proceeded through a reaction sequence involving the formation of an additional intermediate anion $(Ti_8O_{17})^{3-}$ perhaps stabilized by the presence of Nb⁵⁺ ions in the melt.

$$\frac{3}{2}K_{2}O \rightarrow 3K^{+} + \frac{3}{2}O^{2-}$$

$$2TiO_{2} + O^{2-} \rightarrow [Ti_{2}O_{5}]^{2-}$$

$$[Ti_{2}O_{5}]^{2-} + [6TiO_{2}] \rightarrow [Ti_{8}O_{17}]^{2-}$$

$$[Ti_{8}O_{17}]^{2-} + e \rightarrow [Ti_{8}O_{17}]^{3-} \text{ cathode}$$

$$[Ti_{8}O_{17}]^{3-} + 3K^{+} \rightarrow K_{3}Ti_{8}O_{17}$$

$$\frac{1}{2}O^{2-} - e \rightarrow \frac{1}{4}O_{2} \text{ anode}$$

The bronze should, therefore, be crystallized near but not necessarily at the cathode, a supposition which is supported by the observation that crystals of $K_{3}Ti_{8}O_{17}$ were found throughout the cathode compartment. In melts in which $Ti_8O_{17}^2$ polyanions are the stable species, it may be possible to conceive certain acid-base conditions under which the octatitanate M_8^{2+} Ti $_8^{4+}O_{17}$ might form, but such conditions have not yet been found. Electrolysis of K₂Ti₂O₅ melts containing substantial amounts of V_2O_5 produced a new layer titanate $K_xV_xTi_{2-x}O_4$ (19). This compound is structurally related to $K_3 Ti_8 O_{17}$, but it contains infinite sheets of $[M_x O_{2x}]^ (x = \infty)$ polyanions parallel to the 3.8 Å axis with V^{3+} ions randomly distributed with Ti⁴⁺ in the octahedral sites. This may indicate that substitution of Ti⁴⁺ by V³⁺ stabilizes fragments of these large sheets in the melt as ions such as $[M_4O_8]^-$ which join in the solid state into infinite two-dimensional layers. To establish the nature of the species which exist in the various molten alkali metal titanate systems would require their isolation or characterization under varying conditions in the melt, at temperatures near 1000°C. High temperature electrochemical, infrared, and Raman spectroscopic methods have allowed considerable advances in the understanding of the processes taking place in silicate and halide melts, and it may be possible by the application of such techniques to determine if titanate polyanions do form in the molten state.

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